

## Chapter 2 Review Practice Questions

### Transformations of Functions

1. Describe the transformations of the following:

a.  $y - 4 = f(x - 2) + 4$

$$y = f(x - 2) + 4$$

↑      ↑  
2 right + 4 up.

b.  $y = 3f(-2(x - 5)) + 7$

$$y = 3f(-2(x - 5)) + 7$$

VEd 3    HC of 2    5 right    7 up.  
↓ ref. over y-axis

2. Write the mapping notation for the following transformations:

$$y = -f\left(\frac{1}{2}(x - 6)\right) + 2$$

ref in  
x-axis    HEd 2    6 right    2 up

$(2x+6, -y+2)$

3. Given the mapping notation, write the corresponding function in the form of  $y = f(x)$ .

a.  $(x, y) \rightarrow (2x, y - 4)$

HEd 2    4 down     $y = f(\frac{1}{2}x) - 4$

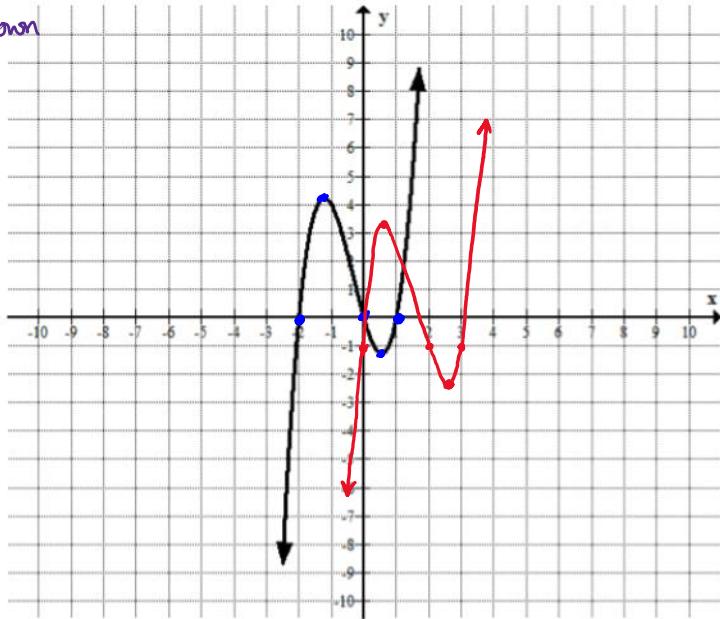
b.  $(x, y) \rightarrow (-x + 3, -2y - 4)$

ref. in  
y-axis    3 right    VEd 2  
+ ref. in  
x-axis    4 down

$y = -2f(-(x-3)) - 4$

4. Given the function  $y = f(x)$  below, perform the following transformations and show your table of values.

$x$	$y$	$x+2$	$y-1$
-2	0	0	-1
-1.3	3	0.7	3.3
0	0	2	-1
0.5	-2	2.5	-2.2
1	0	3	-1



State the domain and range (in set notation).

$$\{x | x \in \mathbb{R}\} \quad \{y | y \in \mathbb{R}\}$$

5. Given the function  $y = |x|$  write the function with the following transformation and, using the point  $(-2, 2)$  from the base function, determine the image point.

a.  $y = f(x-2) + 7$

$(-2, 2)$   
 +2 +7  
 2 right 7 up  
 $\boxed{(0, 9)}$

- b. Vertically translated 9 units down and horizontally translated 3 left

$(-2, 2)$   
 -3 -9  
 $\boxed{(-5, -7)}$

- c. Horizontally translated 5 right and vertically translated 2 up

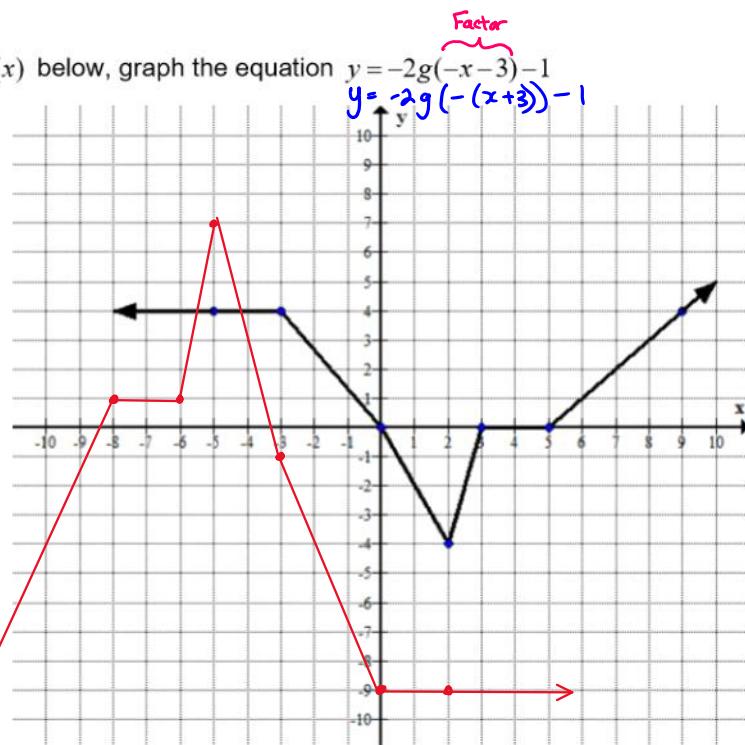
$(-2, 2)$   
 +5 +2  
 $\boxed{(3, 4)}$

6. Given the function  $y = f(x)$  below, graph the equation  $y = -2g(-x-3)-1$

$x$	$y$
-5	4
-3	4
0	0
2	-4
3	0
5	0
9	4

$-x$	$-2y$
5	-8
3	-8
0	0
-2	8
-3	0
-5	0
-9	-8

$-x-3$	$2^{ x }-1$
2	-9
0	-9
-3	-1
-5	7
-6	1
-8	-1
-12	-9



State the domain and range:

$$\{x | x \in \mathbb{R}\} \quad \{y | y \leq 7, y \in \mathbb{R}\}$$

Base  
 $y = x^2$

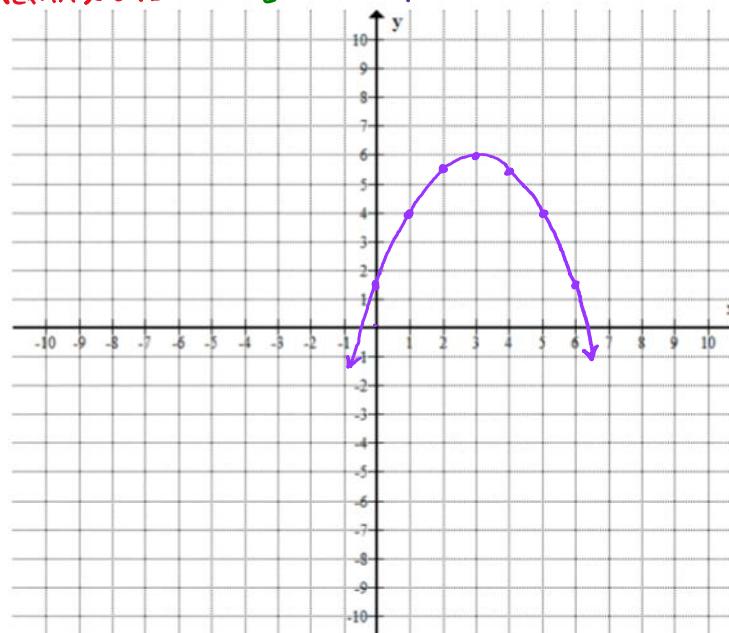
7. Graph the function  $y = -\frac{1}{2}(x-3)^2 + 6$  AND state the domain and range.

$\text{vert } \frac{1}{2} + \text{ref. in } x\text{-axis}$  3 right Up

$x$	$y$
-3	9
-2	4
-1	1
0	0
1	1
2	4
3	9

$x$	$\frac{1}{2}y$
-3	$-\frac{9}{2}$
-2	-2
-1	$-\frac{1}{2}$
0	0
1	$-\frac{1}{2}$
2	-2
3	$-\frac{9}{2}$

$x$	$\frac{1}{2}y+6$
0	$\frac{3}{2}$
1	4
2	$\frac{11}{2}$
3	6
4	$\frac{15}{2}$
5	4
6	$\frac{1}{2}$



State the domain and range:

$$\{x | x \in \mathbb{R}\} \quad \{y | y \leq 6, y \in \mathbb{R}\}$$

8. Write the equation  $y = f(x)$  with the transformations described below:

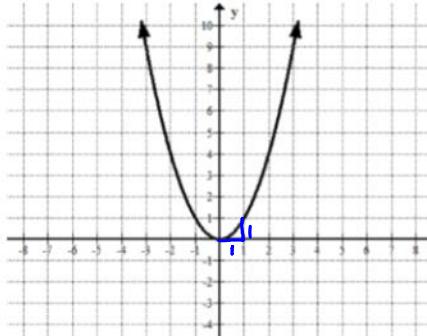
- a. A reflection about the x-axis, vertically compressed by a factor of  $\frac{1}{3}$ , horizontally expanded by a factor of 2, and translated 3 units left and 4 units up.

$$y = -\frac{1}{3}f(\frac{1}{2}(x+3))+4$$

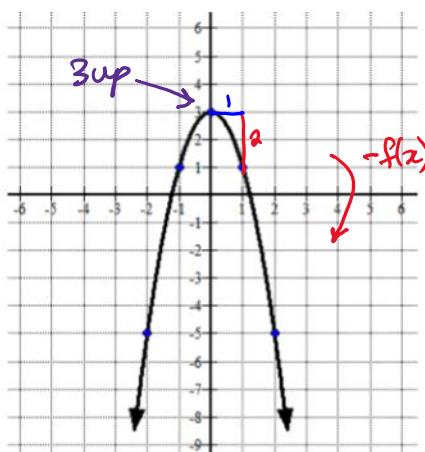
- b. A reflection about the y-axis, vertically expanded by a factor of 2, horizontally compressed by a factor of  $\frac{1}{2}$ , and translated 2 units right and 1 unit down.

$$y = 2f(-2(x-2))-1$$

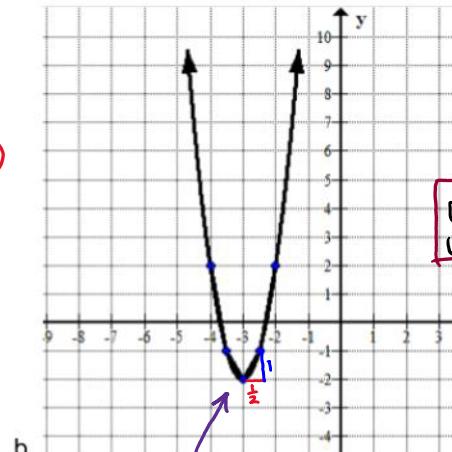
9. Given the following graph of the function  $y = x^2$ , determine the equation of the transformed functions below.



$$y = -2x^2 + 3$$



a.



b.

$$y = f(2(x+3))-2$$

State the domain and range of each:

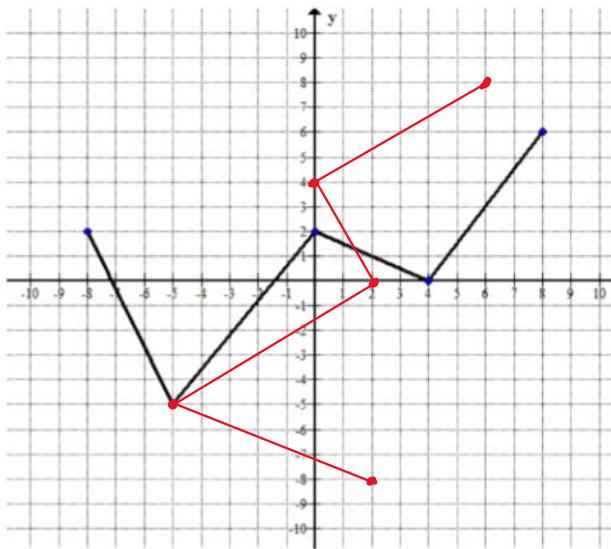
$$\{x | x \in \mathbb{R}\}$$

$$\{y | y \leq 3\}$$

$$\{x | x \in \mathbb{R}\}$$

$$\{y | y \geq -2\}$$

10. Graph the inverse of the given function,  $y = f(x)$ :



$$y = f(x)$$

x	y
-8	2
-5	-5
0	2
4	0
8	6

$$\{x \mid -8 \leq x \leq 8\}$$

$$\{y \mid -5 \leq y \leq 6\}$$

$$y = f^{-1}(x)$$

x	y
2	-8
-5	-5
2	0
0	4
6	8

-5 invariant

$$\{x \mid -5 \leq x \leq 8\}$$

$$\{y \mid -8 \leq y \leq 8\}$$

11. Determine the equation of the inverse for each of the following:

a.  $y = -2x + 3$

$$\begin{aligned} x &= -2y + 3 \\ -3 &\quad \downarrow \\ x-3 &= -2y \\ \frac{x-3}{-2} &= \frac{-2y}{-2} \end{aligned}$$

$$\boxed{f^{-1}(x) = -\frac{x-3}{2}}$$

or  
 $f^{-1}(x) = -\frac{1}{2}x + \frac{3}{2}$

b.  $y = \frac{1}{2}(x-4)^2 - 3$

$$\begin{aligned} x &= \frac{1}{2}(y-4)^2 - 3 \\ +3 &\quad \downarrow \\ 2(x+3) &= \frac{1}{2}(y-4)^2 \\ \sqrt{2(x+3)} &= \sqrt{\frac{1}{2}(y-4)^2} \\ \pm \sqrt{2(x+3)} &= y-4 \\ +4 &\quad \downarrow \\ \boxed{f^{-1}(x) = \pm \sqrt{2(x+3)} + 4} \end{aligned}$$

c.  $y = \sqrt{2x-1} + 4$

$$\begin{aligned} x &= \sqrt{2y-1} + 4 \\ -4 &\quad \downarrow \\ (x-4) &= \sqrt{2y-1} \\ (x-4)^2 &= 2y-1 \\ +1 &\quad \downarrow \\ (x-4)^2 + 1 &= 2y \\ \frac{1}{2} &\quad \downarrow \\ \boxed{f^{-1}(x) = \frac{1}{2}(x-4)^2 + \frac{1}{2}} \\ f^{-1}(x) &= \frac{(x-4)^2 + 1}{2} \end{aligned}$$

d.  $y = \frac{2x}{3x-1}$

$$\begin{aligned} x &= \frac{2y}{3y-1} \\ x(3y-1) &= 2y \\ 3xy - x &= 2y \\ -2y &\quad \downarrow \\ 3xy - 2y &= x \\ \text{factor} & \\ y(3x-2) &= \frac{x}{3x-2} \\ \boxed{f^{-1}(x) = \frac{x}{3x-2}} \end{aligned}$$