

Tuesday, Apr. 2nd

Plan For Today:

1. Any questions about anything?

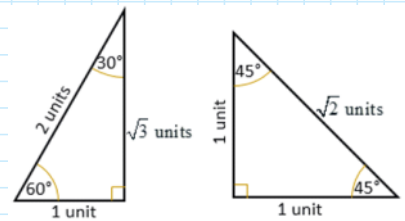
- ◆ *Review 6.1 & part of 6.2 with Check-in quiz*

2. Continue Chapter 6: The Unit Circle & Trigonometry

- ◆ 6.1: Trigonometric Functions
- ◆ **6.2: Trig Functions of Acute Angles**
- ◆ **6.3: Trig Functions of General & Special Angles**
- ◆ 6.4: Graphing Basic Trig Functions
- ◆ 6.5: Applications of Periodic Functions

3. Do Practice Questions from Workbook

4. Do Unit 3 Exponents and logs Rewrite at 12:30pm



	30°	45°	60°
sin	$\frac{1}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{\sqrt{3}}{2}$
cos	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$
tan	$\frac{1}{\sqrt{3}}$	1	$\sqrt{3}$

Plan Going Forward:

1. Finish going through 6.1-6.4 practice questions in textbook.

*** 6.1-6.4 CHECK-IN QUIZ ON THURSDAY, APRIL 4TH**

2. We will finish Chapter 6 (Trigonometry I) on the Thursday and start Chapter 7 (Trig II).

*** CHAPTER 6 PROJECT (PART A HANDOUT & PART B IN DESMOS) DUE TUESDAY, APR. 9TH**

■ <https://student.desmos.com/activitybuilder/student-greeting/65f089483694a5f29f2b2f77>

*** CHAPTER 6 QUIZ ON TUESDAY, APR. 9TH**

Please let me know if you have any questions or concerns about your progress in this course. The notes from today will be posted at anurita.weebly.com after class.
Anurita Dhiman = adhiman@sd35.bc.ca

Apr. 2, 2024

Name: KEY TOTAL = / 9 marks

Check-in Quiz Section 6.1-6.2:
Radian, Degrees, Angles, Arc Length, & Trig Ratios

Complete the following questions SHOWING ALL WORK and steps where applicable.

$180^\circ = \pi$

1. Convert the following angles to degrees or radians. 0.5 marks each = 2 marks

a. $\theta = \frac{5}{150} \times \frac{\pi}{180} = \frac{5\pi}{6}$

b. $\theta = \frac{2\pi}{1.5} \times \frac{180^\circ}{\pi} = 120^\circ$

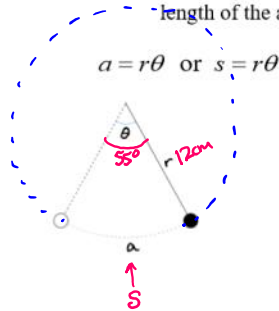
c. $\theta = -\frac{23}{460} \times \frac{\pi}{180} = -\frac{23\pi}{9}$

d. $\theta = -\frac{7\pi}{4.1} \times \frac{180}{\pi} = -315^\circ$

$-\frac{23}{9}\pi \checkmark$

2. A pendulum swings in a frictionless environment forever. If the angle it makes through its swing is 55° and the length of the chain holding the pendulum is 12cm, what is the length of the arc that is produced by the swing of the pendulum?

1 mark



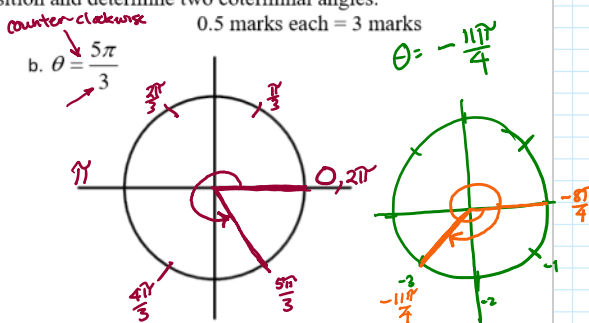
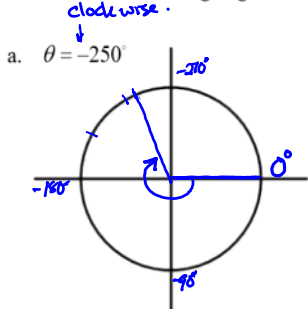
$\theta =$ in radians only.

$55^\circ \times \frac{\pi}{180} = \frac{11\pi}{36}$

$s = 12 \cdot \frac{11\pi}{36} = \frac{11\pi}{3} \text{ cm exact.}$

$= 11.52 \text{ cm. approximate.}$

3. Draw the following angles in standard position and determine two coterminal angles. 0.5 marks each = 3 marks



coterminal angles

$$\theta = -250^\circ + 360^\circ = 110^\circ$$

$$= -250^\circ + 360^\circ(2) = 470^\circ$$

$$\text{OR } -250^\circ - 360^\circ = -610^\circ$$

in general = any coterminal $\rightarrow -250^\circ + 360^\circ n, n \in \mathbb{I}$

coterminal angles

$$\frac{5\pi}{3} + 2\pi n = \frac{5\pi}{3} + \frac{6\pi n}{3} \rightarrow \frac{5\pi + 6\pi n}{3}$$

$$\frac{5\pi}{3} - 6\pi = \frac{5\pi - 36\pi}{3} = \frac{-31\pi}{3}$$

$$\text{any coterminal} = \frac{5\pi}{3} + 2\pi n, n \in \mathbb{I}$$

4. Given that $\cos \theta = \frac{5}{6}$ in Quadrant IV, draw the triangle, determine the hypotenuse of the triangle and determine the exact value of the other trig ratios. 3 marks

$$\cos \theta = \frac{5}{6} \text{ adjacent/hypotenuse, QIV}$$

CAH

reciprocal

$$\sec \theta = \frac{6}{5}$$

SOH

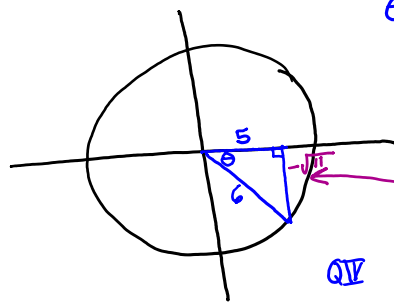
$$\sin \theta = -\frac{\sqrt{11}}{6}$$

$$\csc \theta = -\frac{6}{\sqrt{11}} \rightarrow -\frac{6}{\sqrt{11}} \times \frac{\sqrt{11}}{\sqrt{11}} = -\frac{6\sqrt{11}}{11} \text{ rationalized.}$$

TOA

$$\tan \theta = -\frac{\sqrt{11}}{5}$$

$$\cot \theta = -\frac{5}{\sqrt{11}} \rightarrow -\frac{5}{\sqrt{11}} \times \frac{\sqrt{11}}{\sqrt{11}} = -\frac{5\sqrt{11}}{11} \text{ rationalized.}$$



θ is always next to x-axis!!

pythag:

$$a^2 + b^2 = c^2$$

$$x^2 + y^2 = r^2$$

$$5^2 + y^2 = 6^2$$

$$25 + y^2 = 36 = 25$$

$$\sqrt{y^2} = \sqrt{11}$$

$$y = -\sqrt{11} \text{ in QIV} \leftarrow y = \pm\sqrt{11}$$

p. 258

$$\sin \theta = \frac{y}{r}$$

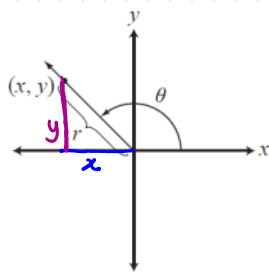
$$\csc \theta = \frac{r}{y}$$

$$\cos \theta = \frac{x}{r}$$

$$\sec \theta = \frac{r}{x}$$

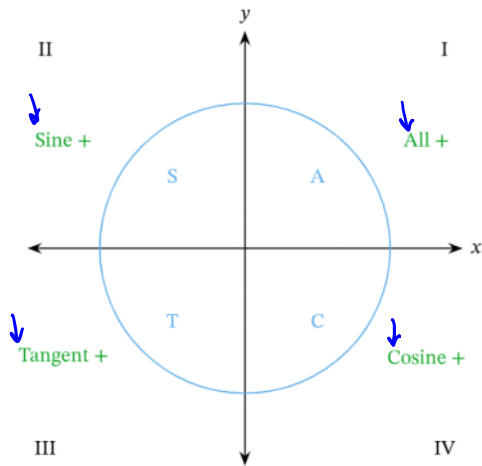
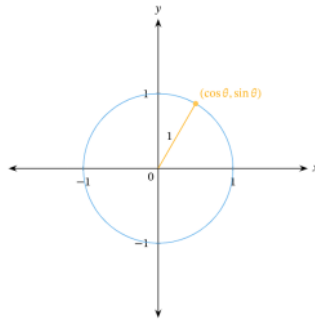
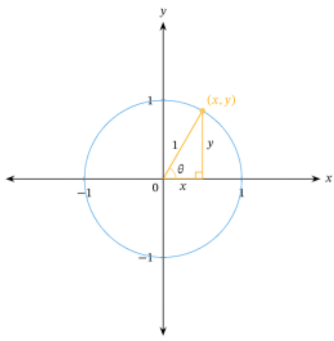
$$\tan \theta = \frac{y}{x}$$

$$\cot \theta = \frac{x}{y}$$



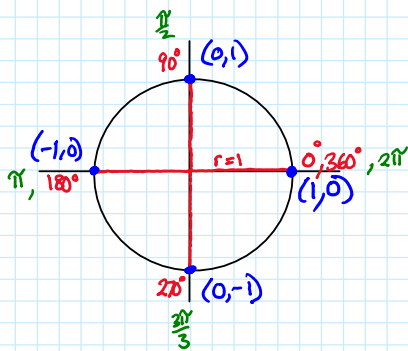
Where $r = \sqrt{x^2 + y^2}$

$$r^2 = x^2 + y^2 \text{ OR } x^2 + y^2 = r^2$$



- Quadrant
- ① All
 - ② Students
 - ③ Take
 - ④ Calculus.

6.3 Quadrant Angles.



$$\cos \theta = \frac{x}{r} = x \rightarrow \cos \theta = x \quad \sec \theta = \frac{r}{x} = \frac{1}{x}$$

$$\sin \theta = \frac{y}{r} = y \rightarrow \sin \theta = y \quad \csc \theta = \frac{r}{y} = \frac{1}{y}$$

$$\tan \theta = \frac{y}{x} \rightarrow \cot \theta = \frac{x}{y}$$

Summary:

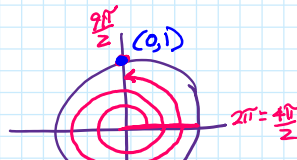
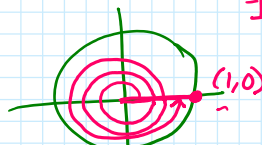
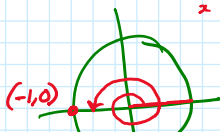
$\cos \theta = x$	$\sec \theta = \frac{1}{x}$
$\sin \theta = y$	$\csc \theta = \frac{1}{y}$
$\tan \theta = \frac{y}{x}$	$\cot \theta = \frac{x}{y}$

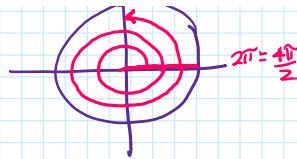
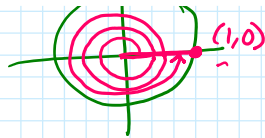
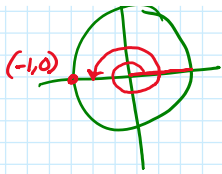
Ex 1

- a) $\cos 0^\circ = \boxed{1}$
- b) $\tan 90^\circ = \frac{1}{0} = \boxed{\text{undefined}}$
- c) $\sin \pi = \boxed{0}$
- d) $\csc \frac{3\pi}{2} = \frac{1}{-1} = \boxed{-1}$

Ex 2

- a) $\underline{\underline{\cos 540^\circ}} = \underline{\underline{-1}}$
- b) $\tan 6\pi = \frac{0}{2} = \underline{\underline{0}}$
- c) $\csc \frac{3\pi}{2} = \frac{1}{-1} = \underline{\underline{1}}$

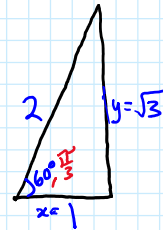
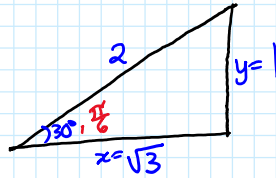
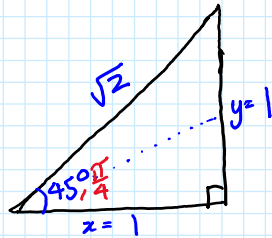




Special Angles

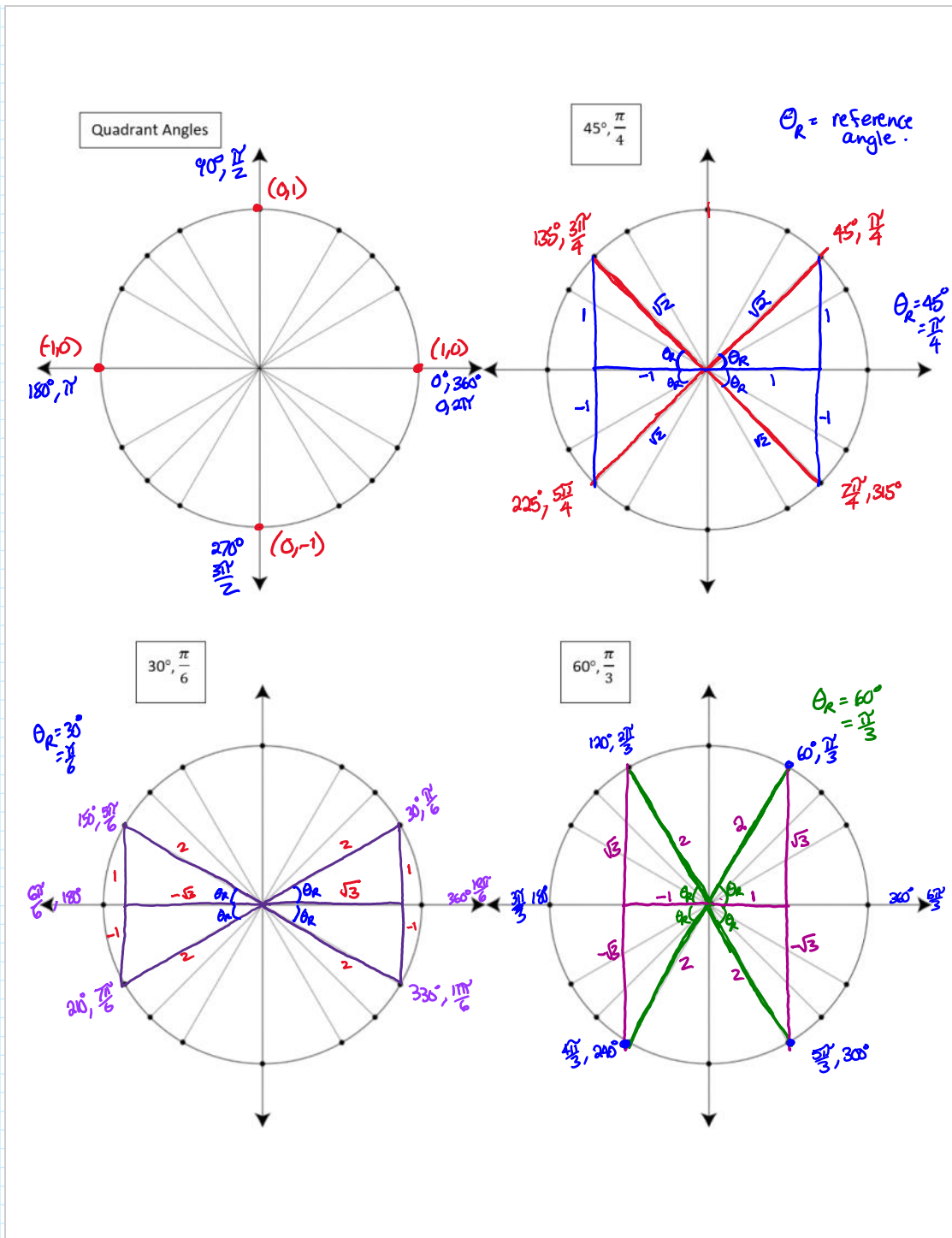
$$30^\circ - 45^\circ - 60^\circ$$

$$\frac{\pi}{6} - \frac{\pi}{4} - \frac{\pi}{3}$$



Reference Angle = acute angle next to x-axis.

↑
90°



p. 20 Ex: 4

Determine exact value of:

a) $\sin 240^\circ$

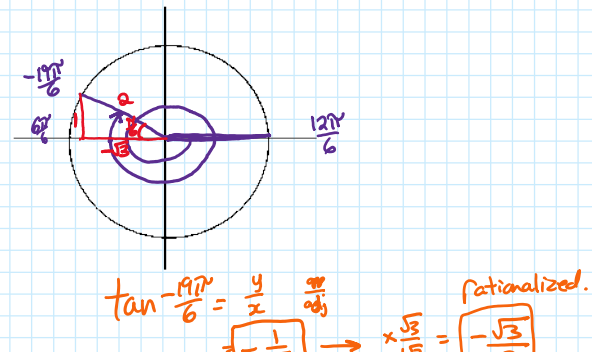
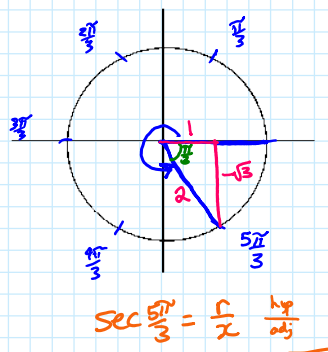
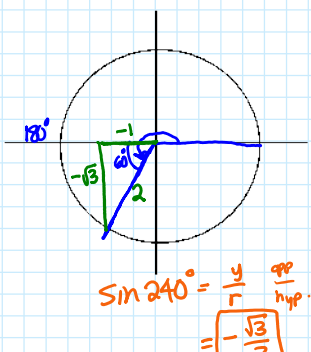
b) $\sec \frac{5\pi}{3}$

c) $\tan(-\frac{19\pi}{6})$

① draw angle in standard position.

② Determine θ_R

③ draw special triangle



③ draw special triangle

④ use triangle to answer question.

$$\sin 240^\circ = \frac{y}{r} = \frac{\text{opp}}{\text{hyp}} = \frac{-\sqrt{3}}{2}$$

$$\sec \frac{5\pi}{3} = \frac{r}{x} = \frac{\text{hyp}}{\text{adj}} = \frac{2}{1} = 2$$

$$\tan^{-1} \frac{1}{\sqrt{3}} = \frac{y}{x} = \frac{\text{opp}}{\text{adj}} \rightarrow \frac{1}{\sqrt{3}} = \frac{1}{\sqrt{3}} \rightarrow \frac{\sqrt{3}}{\sqrt{3}} = \frac{\sqrt{3}}{3} \text{ (rationalized)}$$

Finding θ instead

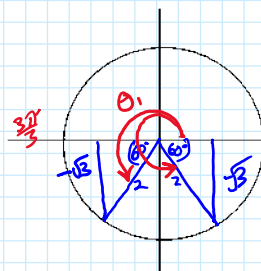
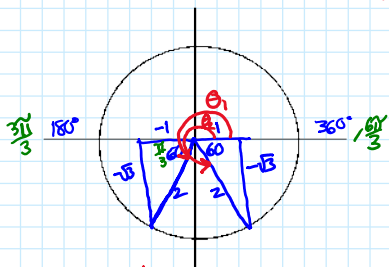
ex: Solve: $\sin \theta = -\frac{\sqrt{3}}{2}$ within $0 \leq \theta < 2\pi$
 $0^\circ \leq \theta < 360^\circ$ } solutions within one rotation of a circle

① $\sin \theta = \frac{y}{r} = \frac{\text{opp}}{\text{hyp}} = -\frac{\sqrt{3}}{2}$ (y/opp, r/hyp)

② (-) \rightarrow sin (-) in QIII & QIV

③ Draw the angles with matching reference angle.

Ex 7 $\csc x = -\frac{2}{\sqrt{3}}$ (r hyp, y opp)
 (-) sin QIII QIV



$$\theta = 240^\circ, 300^\circ$$

$$\theta = \frac{4\pi}{3}, \frac{5\pi}{3}$$

④ determine angles in standard position.

$$\theta_1 = 240^\circ$$

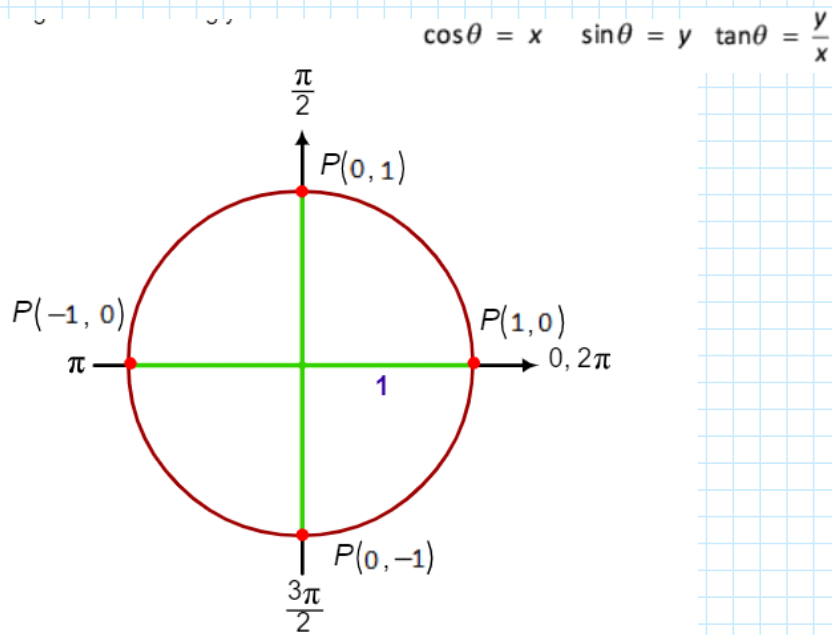
$$\theta_2 = 300^\circ$$

$$\theta_1 = \frac{4\pi}{3}$$

$$\theta_2 = \frac{5\pi}{3}$$

6.3 Trig Functions of General & Special Angles

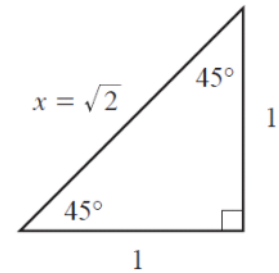
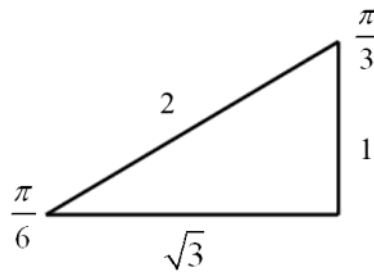
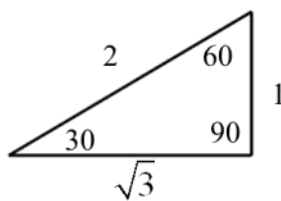
Quadrant Angles



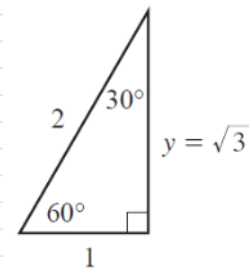
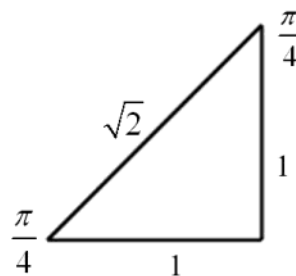
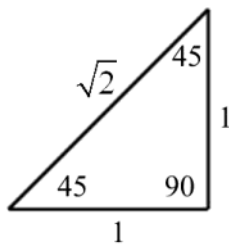
30-45-60 Special Triangles

Also, Two special triangles

30, 60, 90 triangle

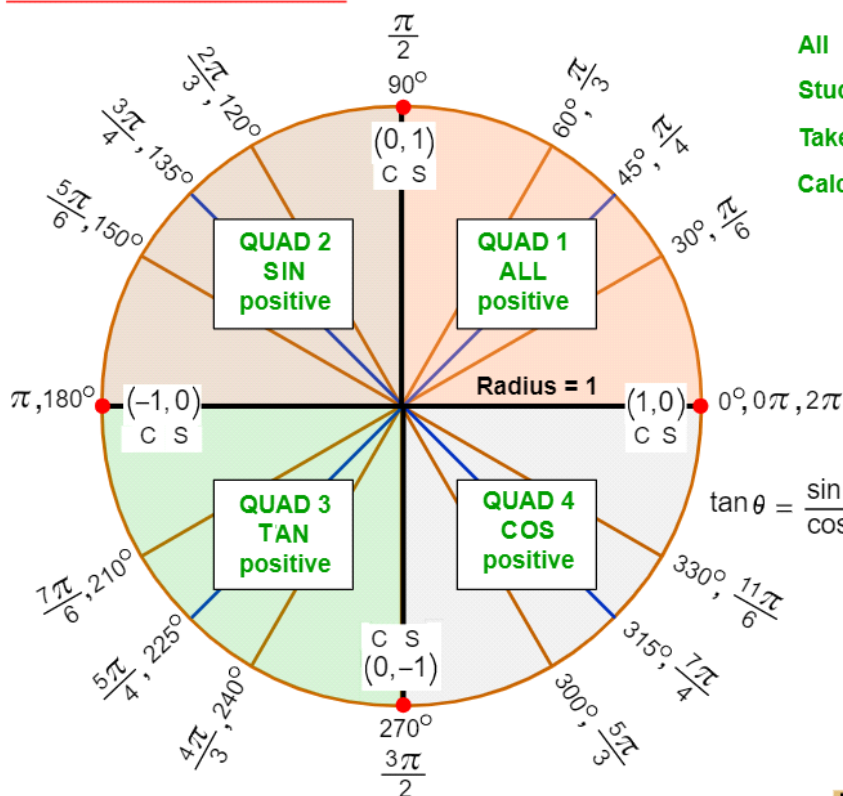


45, 45, 90 triangle



3.6 Exact Values of Special Angles

THE TRIG CIRCLE



All Students Take Calculus

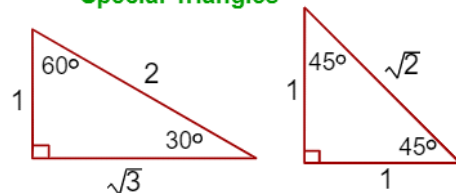
$$\sin = \frac{\text{opp}}{\text{hyp}}$$

$$\cos = \frac{\text{adj}}{\text{hyp}}$$

$$\tan = \frac{\text{opp}}{\text{adj}}$$

$$\tan \theta = \frac{\sin \theta}{\cos \theta} = \frac{S}{C}$$

Special Triangles



	30°	45°	60°
sin	1/2	1/sqrt(2)	sqrt(3)/2
cos	sqrt(3)/2	1/sqrt(2)	1/2
tan	1/sqrt(3)	1	sqrt(3)

Reciprocal Trig Ratios

cosecant $\rightarrow \csc \theta = \frac{1}{\sin \theta}$

secant $\rightarrow \sec \theta = \frac{1}{\cos \theta}$

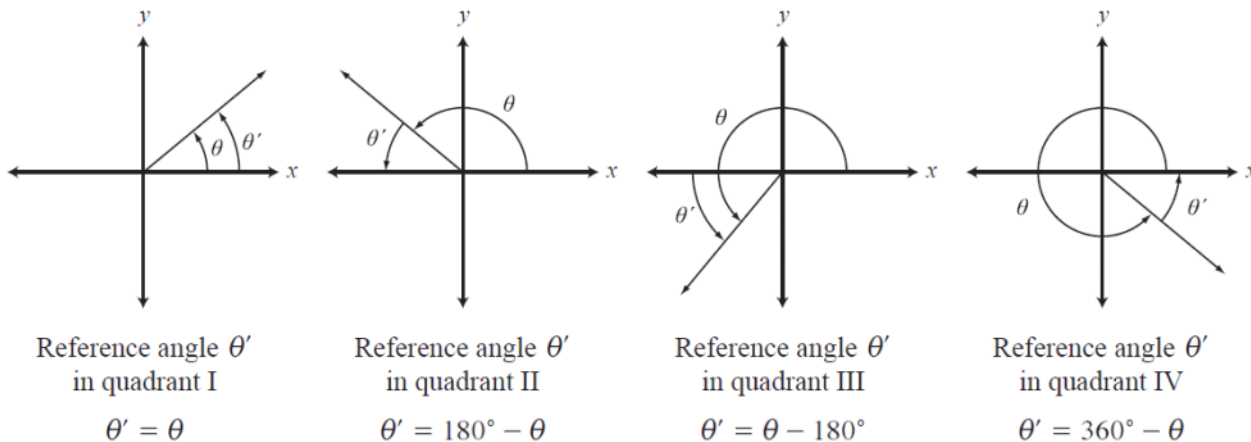
cotangent $\rightarrow \cot \theta = \frac{1}{\tan \theta}$

Reference Angle

Definition of a Reference Angle

For angle θ in standard position, the reference angle is the positive acute angle θ' that is formed with the terminal side of θ and the x -axis.

A reference angle is $0^\circ \leq \theta' \leq 90^\circ$ or $0 \leq \theta' \leq \frac{\pi}{2}$



<https://www.sporcle.com/games/sproutcm/special-angle-trigonometric-match>

<https://www.purposegames.com/game/15c86db5b3>

<https://www.purposegames.com/game/trig-values-level-2-quiz>

Solving Trig Equations Algebraically:

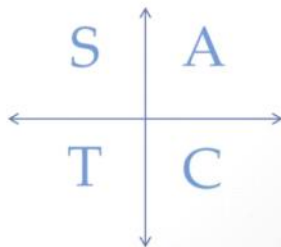
Solving Trig Equations

- When solving trig equations, you will need to get the **trig function** isolated (by itself).
- **Ex:** $2\sin x = 1$ ← **Divide both sides by 2**

$$\sin x = \frac{1}{2} \leftarrow \text{Use unit circle or inverse function on calculator to find angle}$$

We will limit our solutions to $[0, 2\pi)$, and all answers must be in **RADIANS** (π form)

$$30^\circ \text{ and } 150^\circ = \frac{\pi}{6} \text{ and } \frac{5\pi}{6}$$



NOTE

Solving Trigonometric Equations using Quadrants

Trigonometric equations can also be solved **algebraically** using quadrants.

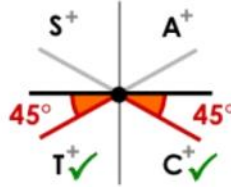
Example

$$\text{Solve } \sqrt{2} \sin x + 1 = 0$$

$$\text{for } 0^\circ \leq x \leq 360^\circ$$

$$\sin x = -\frac{1}{\sqrt{2}}$$

sin negative



∴ solutions are in the 3rd and 4th quadrants

acute angle:

$$\sin^{-1}\left(\frac{1}{\sqrt{2}}\right) = 45^\circ$$

$$\begin{aligned} \therefore x &= 180^\circ + 45^\circ & \text{or} & & x &= 360^\circ - 45^\circ \\ &= \underline{\underline{225^\circ}} & & & &= \underline{\underline{315^\circ}} \end{aligned}$$

